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In[71]:= diffeq = (4 x^2 y''[x]) - (8 x^2 y'[x]) + (((4 x^2) + 1) y[x]) == 0;
sol = DSolve[diffeq, y[x], x]
diffeq2 = (3 x^2 g''[x]) + (2 x g'[x]) + ((x^2) g[x]) == 0;
sol2 = DSolve[diffeq2, g[x], x]
g1[x_] := ((x^(1/6)) BesselJ[1/6, x/Sqrt[3]]) (2^(1/6)) (3^(1/12)) Gamma[7/6];
g2[x_] :=
  ((x^(1/6)) BesselY[1/6, x/Sqrt[3]]) (-Pi) (3^(-1/12)) (Gamma[1/6]^(-1)) / (2^(1/6));
Series[g1[x], {x, 0, 6}]
Series[g2[x], {x, 0, 4}]

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$$\text{Out}[72]= \left\{ \left\{ y[x] \rightarrow e^x \sqrt{x} C[1] + e^x \sqrt{x} C[2] \log[x] \right\} \right\}$$

$$\text{Out}[74]= \left\{ \left\{ g[x] \rightarrow x^{1/6} \text{BesselJ}\left[\frac{1}{6}, \frac{x}{\sqrt{3}}\right] C[1] + x^{1/6} \text{BesselY}\left[\frac{1}{6}, \frac{x}{\sqrt{3}}\right] C[2] \right\} \right\}$$

$$\text{Out}[77]= x^{1/3} - \frac{x^{7/3}}{14} + \frac{x^{13/3}}{728} + O[x]^{19/3}$$

$$\text{Out}[78]= 1 + \frac{\left(\frac{3}{2}\right)^{1/3} \text{Gamma}\left[-\frac{1}{6}\right] x^{1/3}}{2 \text{Gamma}\left[\frac{1}{6}\right]} - \frac{x^2}{10} - \frac{\left(\left(\frac{3}{2}\right)^{1/3} \text{Gamma}\left[-\frac{1}{6}\right]\right) x^{7/3}}{28 \text{Gamma}\left[\frac{1}{6}\right]} + \frac{x^4}{440} + O[x]^{25/6}$$